Algebra 1 – UNIT 2 Linear and Exponential Relationships

Critical Area: Students will learn function notation and develop the concepts of domain and range. They move beyond viewing functions as processes that take inputs and yield outputs and start viewing functions as objects in their own right. They explore many examples of functions, including sequences; they interpret functions given graphically, numerically, symbolically, and verbally, translate between representations, and understand the limitations of various representations. They work with functions given by graphs and tables, keeping in mind that, depending upon the context, these representations are likely to be approximate and incomplete. Their work includes functions that can be described or approximated by formulas as well as those that cannot. When functions describe relationships between quantities arising from a context, students reason with the units in which those quantities are measured. Students explore systems of equations and inequalities, and they find and interpret their solutions. Students build on and informally extend their understanding of integer exponents to consider exponential functions. They compare and contrast linear and exponential functions, distinguishing between additive and multiplicative change. They interpret arithmetic sequences as linear functions and geometric sequences as exponential functions.

CLUSTERS	COMMON CORE STATE STANDARDS				
Extend the properties of exponents to rational	Number and Quantity - The Real Number System				
exponents.	N.RN.1. Explain how the definition of the meaning of rational exponents follows from extending the				
	properties of integer exponents to those values, allowing for a notation for radicals in terms of rational				
	exponents. For example, we define $5^{1/3}$ to be the cube root of 5 because we want $(5^{1/3})^3 = 5^{(1/3)3}$ to hold, so				
	$(5^{1/3})^3$ must equal 5.				
	N.RN.2 Rewrite expressions involving radicals and rational exponents using the properties of exponents.				
Build a function that models a relationship	Functions - Building Functions				
between two quantities.	F.BF.1. Write a function that describes a relationship between two quantities. \star				
Limit to EDE 1 a 1 b and 2 to line and a					
Limit to F.BF.1a, 1b, and 2 to linear and	a. Determine an explicit expression, a recursive process, or steps for calculation from a context.				
exponential functions. In F.BF.2, connect	b. Combine standard function types using arithmetic operations. For example, build a function that				
arithmetic sequences to linear functions and	models the temperature of a cooling body by adding a constant function to a decaying exponential, and				
geometric sequences to exponential functions.	relate these functions to the model.				
	F.BF.2. Write arithmetic and geometric sequences both recursively and with an explicit formula, use them				
	to model situations, and translate between the two forms. \star				
Build new functions from existing functions.	Functions - Building Functions				
	F.BF.3. Identify the effect on the graph of replacing $f(x)$ by $f(x) + k$, $k f(x)$, $f(kx)$, and $f(x + k)$ for specific				
Focus on vertical translations of graphs of	values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and				
linear and exponential functions. Relate the	illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd				
vertical translation of a linear function to its y-	functions from their graphs and algebraic expressions for them.				
intercept. While applying other transformations					
to a linear graph is appropriate at this level, it					
may be difficult for students to identify or					
distinguish between the effects of the other					
transformations included in this standard.					

CLUSTERS	COMMON CORE STATE STANDARDS			
Understand the concept of a function notation.	Functions - Interpreting Functions			
	F.IF.1 . Understand that a function from one set (called the domain) to another set (called the range) assigns			
	to each element of the domain exactly one element of the range. If f is a function and x is an			
	element of its domain, then $f(x)$ denotes the output of f corresponding to the input x. The graph of f			
	is the graph of the equation $y = f(x)$.			
	F.IF.2 . Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.			
	F.IF.3. Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset			
	of the integers. For example, the Fibonacci sequence is defined recursively by $f(0) = f(1) = 1$, $f(n + 1) = f(n) + f(n - 1)$ for $n \ge 1$.			
Interpret functions that arise in applications in	Functions - Interpreting Functions			
terms of a context.	F.IF.4 For a function that models a relationship between two quantities, interpret key features of graphs and			
	tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the			
Focus linear and exponential functions	relationship. Key features include: intercepts; intervals where the function is increasing, decreasing,			
	positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity. \star			
Analyze functions using different	Functions - Interpreting Functions			
representations.	F.IF.7. Graph functions expressed symbolically and show key features of the graph, by hand in simple			
Linear, exponential, quadratic, absolute value, step,	cases and using technology for more complicated cases.			
piecewise-defined.	a. Graph linear and quadratic functions and show intercepts, maxima, and minima.			
	b. Graph square root, cube root, and piecewise-defined functions, including step functions and absolute			
	value functions. \star			
	F.IF.9 . Compare properties of two functions each represented in a different way (algebraically, graphically,			
	numerically in tables, or by verbal descriptions). For example, given a graph of one quadratic function and			
	an algebraic expression for another, say which has the larger maximum.			
Solve systems of equations.	Algebra - Reasoning with Equations and Inequalities			
Linear-linear and linear-quadratic.	A.REI.5. Prove that, given a system of two equations in two variables, replacing one equation by the sum			
	of that equation and a multiple			
	of the other produces a system with the same solutions			
	A.REI.6. Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs			
	of linear equations in two variables.			
Represent and solve equations and inequalities	es Algebra - Reasoning with Equations and Inequalities			
Graphically.	A.REI.10. Understand that the graph of an equation in two variables is the set of all its solutions plotted in			
Linear and exponential; learn as general principle.	the coordinate plane, often forming a curve (which could be a line).			
	A.REI.11 . Explain why the x-coordinates of the points where the graphs of the equations $y=f(x)$ and $y=g(x)$			
	intersect are the solutions of the equation $f(x) = g(x)$ find the solutions approximately, e.g., using			
	technology to graph the functions, make tables of values, or find successive approximations. Include cases			
	where $f(x)$ and/ or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic			
	functions. ★			

COMMON CORE STATE STANDARDS				
A.REI.12. Graph the solutions to a linear inequality in two variables as a half-plane (excluding the				
boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in				
two variables as the intersection of the corresponding half-planes.				
Emphasize Mathematical Practices 1, 2, 4, and 7 in this unit.				
LEARNING PROGRESSIONS				
CDE Progress to Algebra K-8				
Progression on HS Math -				

(m)Major Clusters – area of intensive focus where students need fluent understanding and application of the core concepts.

(s)Supporting/Additional Clusters – designed to support and strengthen areas of major emphasis/expose students to other subjects.

★Indicates a modeling standard linking mathematics to everyday life, work, and decision-making.

(+) Indicates additional mathematics to prepare students for advanced courses.

ENDURING UNDERSTANDINGS		ESSENTIAL QUESTIONS		KEY VOCABULARY
٠	Write in equivalent forms that represent both linear and	1.	How will students identify the different parts of a two-	arithmetic Sequence
	exponential functions and construct functions to describe		system equation and explain their meaning within the	asymptote
	the situation and to find solutions		context of the problem?	boundary
٠	Apply rules that builds a function that models a	2.	What is the importance of identifying the structure of	coefficients
	relationship between two quantities		functions and using different ways to represent them?	domain
•	Represent equations and inequalities in one variable in	3.	Why is it important to identify and extend the	exponential
	various ways and use them to extend the properties of		properties of exponents to rational exponents?	explicit
	exponents to rational exponents	4.	When do students decide the best method to solve an	function
•	Understand the relationship between quantities of two		inequality?	geometric Sequence
	systems of equations and the methods to solve two system	5.	How do you know which method to use in solving a	in-equalities
	of linear equations		system of equations?	linear
		6.	Why is it important to analyze functions using different	range
•	Model with linear and exponential functions.		representations?	rate of change
•	Systems of equations compare at least two different	7.	How do I analyze algebraic equations/inequalities to	rational
	functions.		solve problems?	recursively

ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	KEY VOCABULARY
 Vertical translations graphically move lines and curves around the y-intercept. Functions grow by equal differences over equal intervals while exponential functions grow by equal factors over equal intervals. A function is an inequality because it describes a relationship between values of variables with more than a one-to-one correspondence. The parameters of a function are defined by the situational context it models. 	 8. What must students understand in order to create equations that describe numbers or relationships? 9. How do students know the most efficient ways to build a function that models a relationship between two quantities? 10. Why is it important to understand solving a system of linear and exponential relationships in two variables algebraically and graphically? 11. Is there functional relationship in non-linear and ambiguous data? 12. What is the difference in linear and exponential functions and how is that represented graphically? 13. What real-life situations would need exponential or linear function functions to describe them? 14. What is the relationship of a recursive function on the table and graph that represents it? 15. How might an arithmetic sequence be connected to a linear function? 16. How might a geometric sequence be connected to an exponential function? 	symmetries

RESOURCES	INSTRUCTIONAL STRATEGIES	ASSESSMENT
 RESOURCES LAUSD Adopted Textbooks and Programs Big Ideas Learning - Houghton Mifflin Harcourt, 2015: Big Ideas Algebra I College Preparatory Mathematics, 2013: Core Connections, Algebra I The College Board, 2014: Springboard Algebra I 	Use Analogy in the Context of the Math Exponential Growth. When a quantity grows with time by a multiplicative factor greater than 1, it is said the quantity grows exponentially. Hence, if an initial population of bacteria, P_0 , doubles each day, then after t days, the new population is given by $P(t) = P_0 2^t$ This expression can be generalized to include different	ASSESSMENT Formative Assessments <u>http://www.ccsstoolbox.com/parcc/PARCCPrototype</u> <u>main.html</u> • Cellular growth: F-LE.2 and F-BF.2 • Rabbit populations: F-LE. 2 and 5
Materials: Engage New York http://www.engageny.org/sites/default/files/resource/attac hments/algebra-i-m1-copy-ready-materials.pdf Illustrative Mathematics • Skeleton Tower – F. BF.1a	growth rates, as in $(t) = P_0 r^t$. The following example illustrates the type of problem that students can face after they have worked with basic exponential functions like these.	LAUSD Assessments The district will be using the SMARTER Balanced Interim Assessments. Teachers would use the Interim Assessment Blocks (IAB) to monitor the progress of students. Each IAB can be given twice to show growth over time.
• <u>A Sum of Functions</u> – F. BF. 1a	covered by the algae doubles every day. If it continues to	State Assessments

RESOURCES	INSTRUCTIONAL STRATEGIES	ASSESSMENT
 <u>Lake Algae</u> – F. BF.1a <u>Logistic Growth Model, Explicit Version</u>: F-IF.4 Inside Mathematics <u>http://www.insidemathematics.org/index.php/tools-for-teachers/course-1-algebra</u> Tools for algebra Math Assessment Project (MAPS) <u>Building and Solving Equations 2</u>: A-REI <u>Manipulating Radicals</u>: N-RN 	INVECTIONAL STRATEORSgrow unabated, the lake will be totally covered and the fishin the lake will suffocate. At the rate it is growing, this willhappen on June 30.a. When will the lake be covered halfway?b. Write an equation that represents the percentage of thesurface area of the lake that is covered in algae as a functionof time (in days) that passes since the algae was introducedinto the lake.Facilitate a discussion that would direct students to generaterecursive formula for the sequence $P(n)$, which gives thepopulation at a given time period n in terms of thepopulations of bacteria can double every 6 hours under idealconditions, at least until the nutrients in its supporting cultureare depleted. This means apopulation of 500 such bacteria would grow to 1000, etc.Use of Exit Slips to assess student understanding.http://daretodifferentiate.wikispaces.com/Pre-Assessment EPR) strategies for whole group instruction.Strategies to check for understanding: Individual White	California will be administering the SMARTER Balance Assessment as the end of course for grades 3-8 and 11. There is no assessment for Algebra 1. The 11th grade assessment will include ítems from Algebra 1, Geometry, and Algebra 2 standards. For examples, visit the SMARTER Balance Assessment at: http://www.smarterbalanced.org/
	Boards, Fist of Five, Exit Slip, etc.	

LANGUAGE GOALS for low achieving, high achieving, students with disabilities and English Language Learners						
Students will be able to justify (orally and in writing) their rat	Students will be able to justify (orally and in writing) their rationale for solving a system of equations using various methods.					
Example: To solve these equations, I use	instead of	because	·			
Students will be able to explain (writing/speaking/listening		of the quantity represented in terms of t	heir context.	ļ		
<i>Example:</i> $3x - 9y = 5$ and $y = 1/3 x + 1$	·					
				ļ		
Students will be able to read a word problem and identify the language needed to create an algebraic representation.						
Students will be able to explain (orally and in writing) and justify their rationale for their choice of method to solve inequality equations.						
Example: To solve this inequality, I use	because	•				
Students will be able to describe their understanding (orally and in writing) of math vocabulary related to expressions and equations.						
bludents will be able to describe their understanding (orany a	ind in writing) of main vocabulary related	d to expressions and equations.				

LAUSD Secondary Mathematics

Illustrative Mathematics

- <u>Influenza Epidemic</u> : F.IF.4
- Logistic Growth Model, Abstract Version : F.IF.4
- <u>How is the Weather</u>?: F.IF.4
- <u>Telling a Story With Graphs</u> : F.IF.4

LAUSD Concept Lessons

• <u>Tying the Knots</u>

Mathematics Assessment Project Formative Assessments/ Tasks

- <u>Comparing Investment</u> F.LE 1-5.
- <u>Fuctions and Everyday</u> F.BF.1 and F.LE.1-5 :

	DIFFERENTIATION						
	UDL/FRONT LOADING		ACCELERATION		INTERVENTION		
•	Prerequisites Students apply their understanding of the properties of exponents.	•	Students will design a word problem that reflects the use of graphing inequalities.	•	Use real-word context examples to demonstrate the meaning of the parts of a system of equations for the students.		
•	Students apply and extend their knowledge of rational numbers to exponents and to find the values of numerical values that include those numbers.	•	Students will write a real-life scenario and explain the process needed to solve a system of linear equations with two variables.	•	Use of visual interactive websites that through the manipulation of graphs represent inequalities.		
•	Students apply their knowledge about the meaning of the representation of radicals with rational exponents.	•	Student will create a real world problem where students will build a function that model a relationship between two quantities.	•	Students find it useful through technology to recognize functions that represents the same relationship.		
•	Students will understand that if the two sides of one equation are equal, and the two sides of another equation are equal, then the sum (or difference) of these is equal.	•	Students will explain the relationship of properties of exponents to exponential functions. Students will compare and contrast the properties of a linear equation and linear inequality equation.	•	Provide a situation that uses realia to demonstrate how to build a function to model a relationship between two quantities.		
•	Students will extend their knowledge of learning the relationship between the algebraic representation and its graph.	•	Students discuss the following question: Which quantity will grow more rapidly; one that is				
•	Students will use their prior knowledge of creating tables of values for function to find a solutions.		increasing exponentially, one that is increasing quadratically or one that is increasing linearly?				
•	Students will extend their prior knowledge of graphing two equations and be able to interpret the intersections of the graph as the solution to the original equation.						